



Introducing Cosmology

講師資訊

吳志剛

- 現職：
 - 臺北市立天文科學教育館研究組組長
 - 東吳大學物理系
 - 國立故宮博物院講師
 - 國立科學教育館天文講師
 - 國際地球科學奧林匹亞競賽培訓輔導教師
 - 各社大課程規劃委員及講師
- 經歷：中央研究院天文與天文物理研究所
- TEL：(02)28314551 ext 301
- E-mail：astrowu@tam.gov.tw
- FB：https://www.facebook.com/astrowu.tam

What is the Universe?

- When?
- How?
- Size?
- Shape?
- What?
- Where?

遠古神話

屈原

中世紀
歐洲

文藝復興

布魯諾

牛頓

萊布尼茲

開放、無限

封閉、有限

亞里斯多德

楊雄

但丁

愛因斯坦

時間

Cosmology

- Why? Philosophy
- Who? Theology



First Qualitative Cosmology: Newton-Bentley Exchange



1643 – 1727

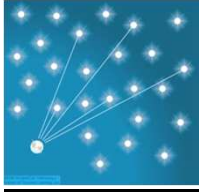
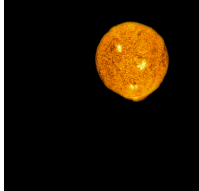


1662 – 1742

Newton's Static Universe

- Universe is **static** and composed of an infinite number of stars that are scattered randomly throughout an **infinite** space.
- Universe is **infinitely old** and will **exist forever** without any major **changes**.
- **Time** and **Space** are **steady** and **independent** of one another and any **objects** in existence within them.

Olbers's Paradox

Why is the sky dark at night?
(Kepler, 1610. Olbers, 1823)

If the universe is infinite, then every line of sight should end on the surface of a star at some point.
⇒ The night sky should be as bright as the surface of stars!

Solution to Olbers's Paradox:
Allan Poe(1848, Eureka), Kelvin(1901)

If the universe had a beginning, then we can only see light from galaxies that has had time to travel to us since the beginning of the universe.
⇒ The **visible** universe is **finite**!

About the Edge of the Universe: Newton-Leibniz-Kant Debate







1646 – 1716
1724 – 1804

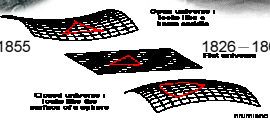
- edged, finite
- no edge, infinite
- finite, edged
- infinite, no edge

1. Stable system
2. No center
3. Infinite(Euclidean space) → insoluble

Curved Space: Gauss and Riemann

1777 – 1855
1826 – 1866 (1854)



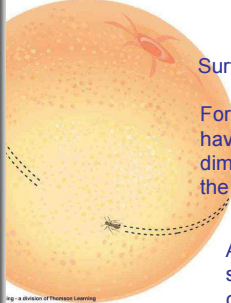
Finite, but without Edge?

2-dimensional analogy
Surface of a sphere

Surface is **finite**, but has **no edge**.

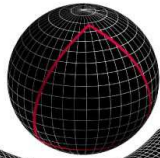
For a creature living on the sphere, having no sense of the third dimension, there's **no center** (on the sphere!): All points are equal.

Alternative: Any point on the surface can be defined as the center of a coordinate system.

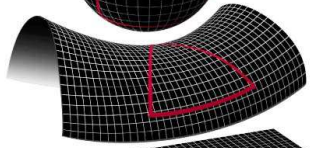


Curvature: the shape of Universe

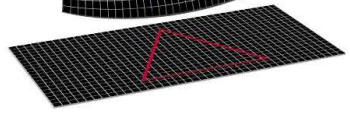
$\Omega_0 > 1$



$\Omega_0 < 1$



$\Omega_0 = 1$




MAP990006

The New Physics

- Special Relativity, 1905
- General Relativity, 1915

$$R_{\mu\nu} - \frac{1}{2} R g_{\mu\nu} = \frac{8\pi G}{c^4} T_{\mu\nu}$$

- Solutions in General Relativity
 - Schwarzschild, 1916
 - Einstein, 1917
 - cosmological constant
 - Friedmann & Lemaître, 1922, 1931
 - Einstein & de Sitter, 1932



1879 – 1955

Hubble's Law

Galaxy	Distance (Mpc)	Recession Velocity (km/s)
Vergo	17.8 Mpc	1,200 km/s
Ursa Major	21.5 Mpc	15,000 km/s
Coma Berenices	310 Mpc	22,000 km/s
Bootes	567 Mpc	39,000 km/s
Hydra	960 Mpc	61,000 km/s

Unshifted position of calcium line

Distant galaxies are receding from us with a speed proportional to distance. $v = H_0 D$ (1929)

Vesto Slipher
1889–1953

Henrietta Leavitt
1875–1969

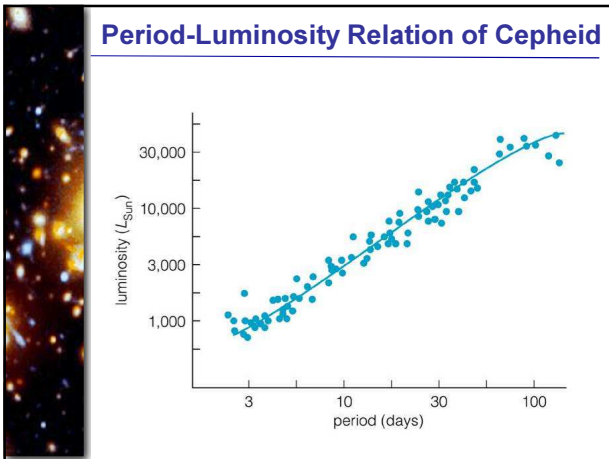
1868–1921

Doppler Effect and Redshift

$$z \equiv \frac{\Delta\lambda}{\lambda} = \frac{\lambda - \lambda_0}{\lambda_0} \approx \frac{v}{c}$$

- Doppler effect
- Cosmological redshift
- Gravitational redshift

UNSHIFTED
REDSHIFTED
BLUESHIFTED



Density parameter Ω , Curvature and destiny of Universe

$$v = H_0 R$$

$$v_c = \sqrt{\frac{2GM}{R}}$$

$$M = \frac{4\pi}{3} R^3 \rho_0$$

$$\Rightarrow \rho_c = \frac{3H_0^2}{8\pi G}$$

if $v > v_c \Rightarrow \rho_c > \rho_0$...**A**

if $v < v_c \Rightarrow \rho_c < \rho_0$...**B**

if $v = v_c \Rightarrow \rho_c = \rho_0$...**C**

$$\Omega = \rho_0 / \rho_c$$

$\rho_c \approx 9 \times 10^{-27} \text{ kg/m}^3$

- negative curvature
open, infinite
expand forever
- positive curvature
closed, finite
expand to shrink
- flat universe
open, infinite
expand forever

The Expanding Universe

- On large scales, galaxies are moving apart, with velocity proportional to distance.
- It's not galaxies moving through space.
- Space is expanding, carrying the galaxies along!
- The galaxies themselves are not expanding!

Expanding Space

Analogy:
A loaf of raisin bread where the dough is rising and expanding, taking the raisins with it.

Misconception:
What is the Universe expanding into?
Where is north of the North Pole?

The Expanding Universe

This does not mean that we are at the center of the universe!

You have the same impression from any other galaxy as well.

The Necessity of a Big Bang

If galaxies are moving away from each other with a speed proportional to distance, there must have been a beginning, when everything was concentrated in one single point:

The Big Bang!
The Big Stretch!

The Age of the Universe

Knowing the current rate of expansion of the universe, we can estimate the time it took for galaxies to move as far apart as they are today:

time = distance / velocity

$v = H_0 D$

$H_0 = 67.80 \pm 0.77$ Mpc/km/s (Planck, 2013)

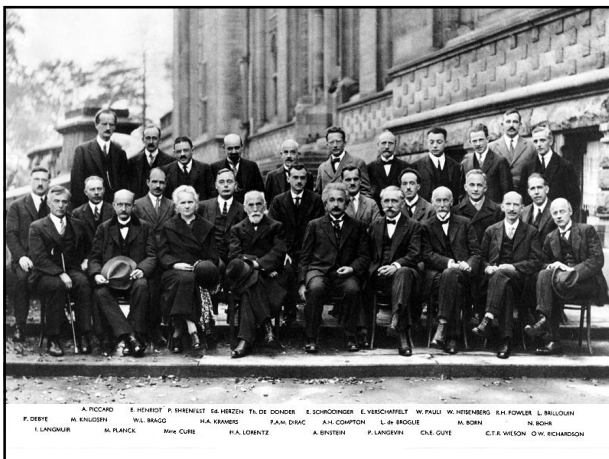
$t \approx d/v = 1/H \sim 13.8$ billion years

Hubble time
It's a estimated age!

Lemaître and Primeval Atom

1894-1966

- Derived Hubble's law, but not linear relation, 1927
- Published "Hypothesis of the Primeval Atom" in Nature, 128 [1931Natur.128..704L](https://doi.org/10.1038/128704L)
- Propose the expansion of the Universe was accelerating, 1931



α β γ & Cosmic Background Radiation

George Gamow 1904-1968 **Ralph Alpher** 1921-2007 **Hans Bethe** 1906-2005 **Robert Herman** 1914-1997

- Advocate and developer of Lemaître's Big Bang
- Modeling the creation of elements, 1942
- Hot Big Bang & CBR~50K, 1946
- Dicke and Peebles: Helium abundance → hot early Universe → blackbody radiation field, 1946
- Alpher and Herman: CBR~5K, 1948

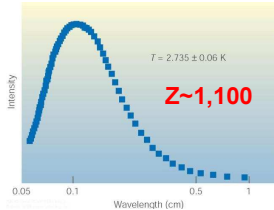
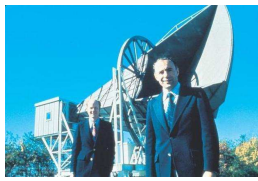
Cosmic Background Radiation

The radiation from the very early universe should still be detectable

Wilson (1936-) & Penzias (1933-)

discovered blackbody radiation with $T = 2.73$ K ($dE_\lambda/d\lambda = 1.063$ mm, 160 GHz, Microwave)

be awarded the Nobel Prize for Physics in 1978



CMB: Modern Ether Drift Experiments

George Smoot

1945-

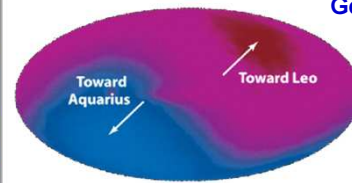
$$l = 245^\circ \pm 15^\circ$$

$$b = 54^\circ \pm 10^\circ$$

$$V = 390 \pm 60 \text{ km/s}$$

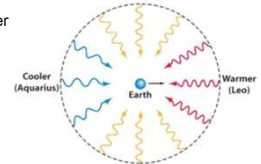
$$\Delta T = 0.00337 \text{ K}$$

$$V = 371 \text{ km/s}$$

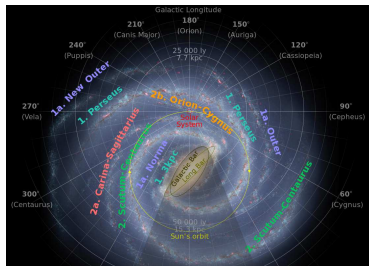


DMR

Differential Microwave Radiometer

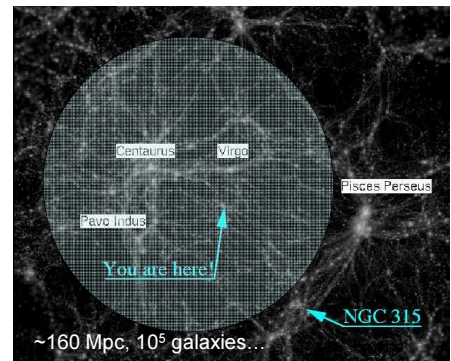


Galactic Particular Velocity



- Earth's Rotation: $0-0.465$ km/sec
- Earth orbits around the Sun: 29.786 km/sec
- Sun orbits around the Galaxy: 250 km/sec
- CMB value: ~ 620 km/sec

Earth's new address: Solar System, Milky Way, Laniakea



CMB: Modern Ether Drift Experiments

Vera Rubin

1928-

- Started to develop an interest in astronomy since 10.
- BA at Vassar College, enroll at Princeton but be denied.
- "galaxies might be rotating around unknown centers, rather than simply moving outwards, as suggested by the Big Bang theory" (Master at Cornell U, 1951).
- "galaxies clumped together, rather than being randomly distributed" (Georgetown U. PhD, 1954).
- Galaxy rotation problem: Dark Matter (1970-1980).

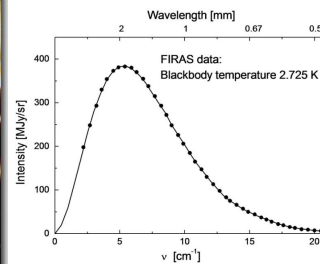


COBE look at the CMB

COsmic **B**ackground **E**xplorer (November 18, 1989)

Principal Investigators

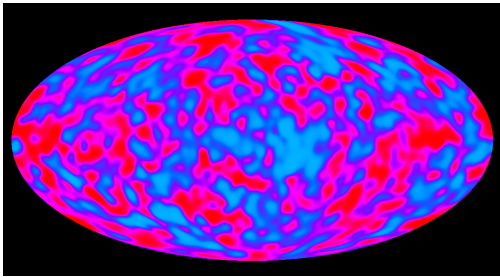
George Smoot, John Mather



FIRAS

Far Infrared Absolute Spectrophotometer

Cosmology's Holy Grail



COBE detected **anisotropies** at the level 100 μK of the CMB. The density fluctuations are believed to have produced structure formation.

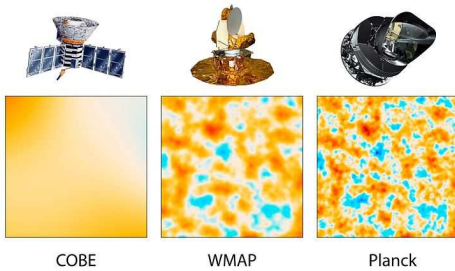
The Nobel Prize in Physics 2006

"for their discovery of the blackbody form and anisotropy of the cosmic microwave background radiation".



John C. Mather
NASA Goddard Space Flight Center, Greenbelt, MD, USA,
George F. Smoot
University of California, Berkeley, CA, USA

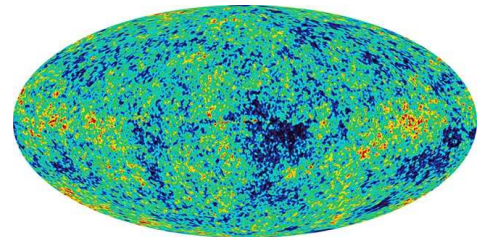
COBE, WMAP, Planck Comparison



Ever-increasing resolution of our maps of the cosmic microwave background radiation from COBE launched in 1989 to WMAP in 2001 (30x better resolution than COBE) to Planck in 2009 (2.5x better than WMAP)

Cosmology with the Cosmic Microwave Background

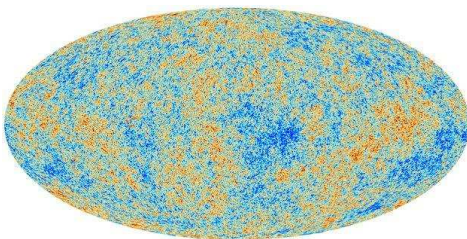
If the universe were perfectly homogeneous on all scales at the time of recombination ($z = 1100$), then the CMB should be perfectly isotropic over the sky.



Instead, it shows small-scale fluctuations:

Planck Reveals an Almost Perfect Universe

The image is based on the initial 15.5 months of data from Planck and is the mission's first all-sky picture of the oldest light in our Universe



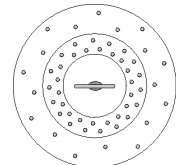
Cosmic microwave background seen by Planck

The Cosmological Principle

Considering the largest scales in the universe, we make the following fundamental assumptions:

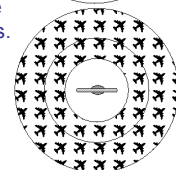
Homogeneity

the local universe has the same physical properties throughout the universe.



Isotropy

the local universe looks the same in any direction that one observes.



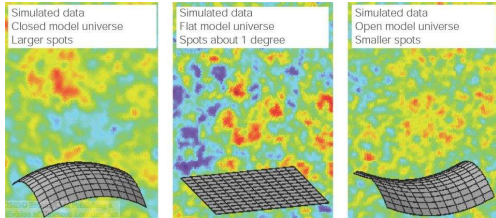
Universality

the laws of physics are the same everywhere in the universe.

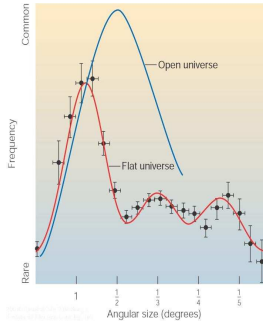
Fluctuations in the Cosmic Microwave Background

The angular size of the CMB fluctuations allows us to probe the geometry of space-time!

CMB fluctuations have a characteristic size of 1 degree.

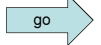


Analysis of the Cosmic Background Fluctuations

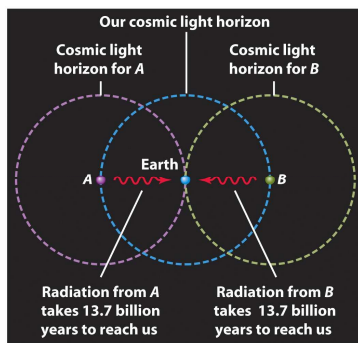


Analyze frequency of occurrence of fluctuations on a particular angular scale

→ Universe has a flat geometry

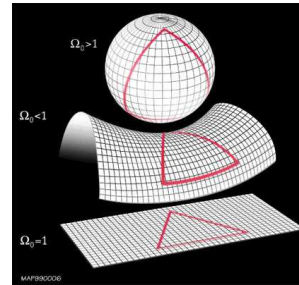


The Isotropy (Horizon) Problem

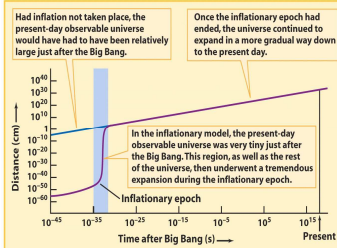


The Flatness Problem

Ω very close to 1, $|\Omega-1| < 0.01$ currently, 10^{-62} at the Planck era.



Inflationary theory



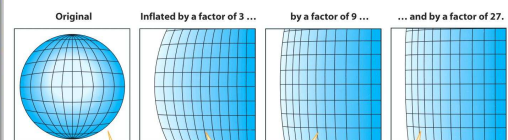
Alan Guth



$10^{-36} \sim 10^{-32}$ second,
expand $10^{20} \sim 10^{30}$

1947~, 1979

Inflation explains why the universe is nearly flat and the 2.725 K microwave background is almost perfectly isotropic

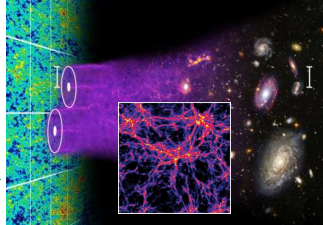


As the sphere is inflated, its curvature eventually becomes undetectable and its surface appears flat.

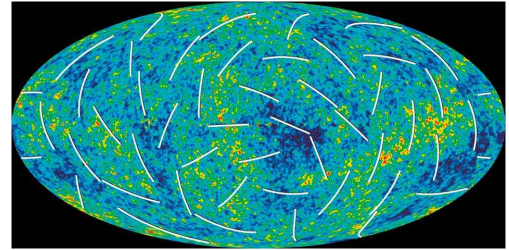
Baryon Acoustic Oscillations

quantum fluctuation during inflation → higher density of plasma → radiation pressure from the photons resists the gravitational compression → sound waves propagate in the universe, last to recombination era. (~37,6000 years) → large scale structures formed from density fluctuations.

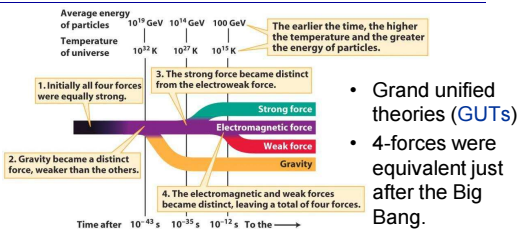
- size of Universe ~ 27.6 Mpc at that time
- major oscillation angular angle ~ 1°
- oscillation ~ 150 Mpc at present



Evidence of Inflation: Polarization of CMB

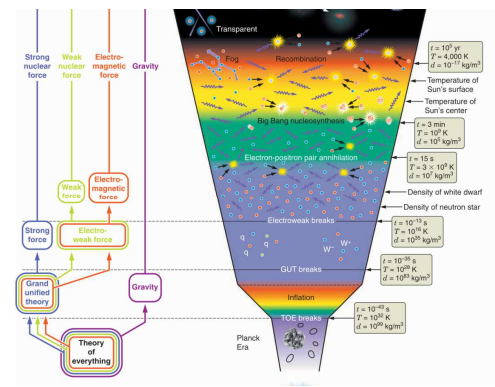


The Fundamental Force of Nature

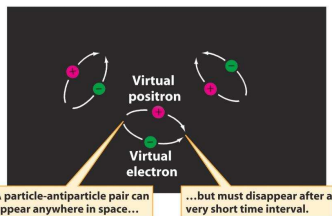


Force	Relative strength	Particles exchanged	Particles on which the force can act	Range	Example
Strong	1	gluons	quarks	10 ⁻¹⁵ m	holding protons, neutrons, and nuclei together
Electromagnetic	1/137	photons	charged particles	infinite	holding atoms together
Weak	10 ⁻⁶	intermediate vector bosons	quarks, electrons, neutrons	10 ⁻¹⁶ m	radioactive decay
Gravitational	6 × 10 ⁻³⁹	gravitons	everything	infinite	holding the solar system together

Evolution of the Universe



Quantum Mechanics and Heisenberg's Uncertainty Principle



$$\Delta E \times \Delta t = \frac{h}{2\pi}$$

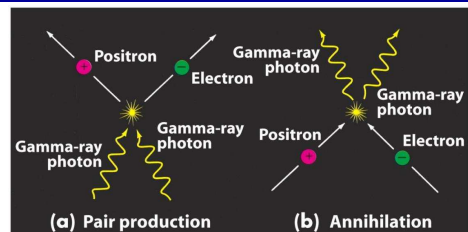
$$\Delta m \times \Delta t = \frac{h}{2\pi c^2}$$

$$\Delta t = \frac{1}{\Delta m} \frac{h}{2\pi c^2} = 6.43 \times 10^{-22} \text{ s}$$

$$\Delta E = \Delta m \times c^2$$

ΔE = uncertainty in energy
 Δt = time interval over which energy is measured
 h = Planck's constant = 6.625×10^{-34} J s

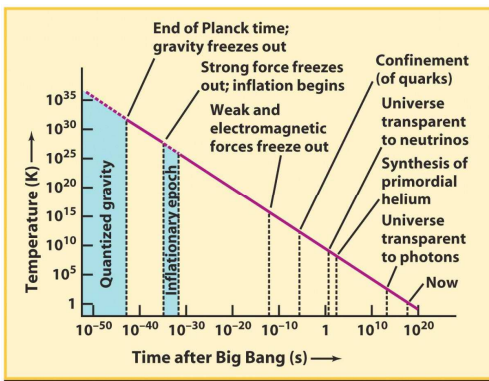
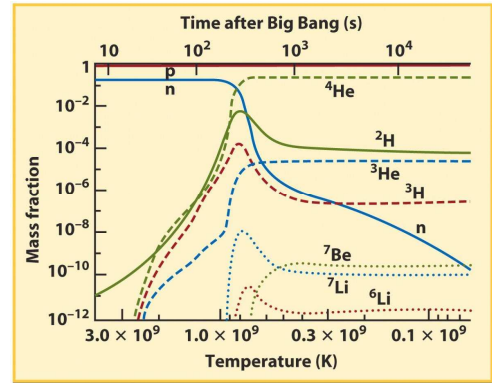
Matter and Antimatter, Pair Production and Annihilated



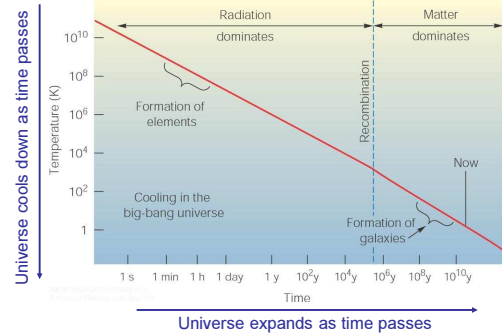
- A virtual pair can become a real particle-antiparticle pair when high-energy photons collide
- In this process, called pair production, the photons disappear, and their energy is replaced by the mass of the particle-antiparticle pair
- In the process of annihilation, a colliding particle-antiparticle pair disappears and high energy photons appear

The Early History of the Universe

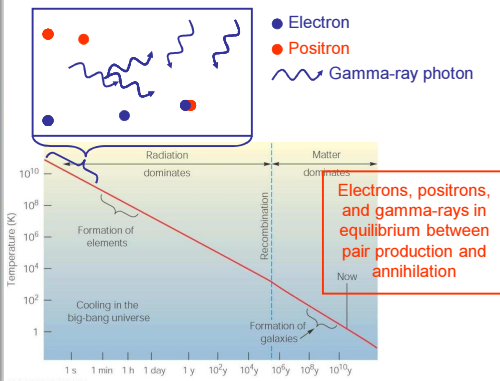
- $t=10^{-6}$ s, $T=10^{13}$ K, $E=1$ GeV. After **Quark confinement period**: proton and neutron appear.
- $t=1$ s, $T=6 \times 10^9$ K, electron and positron appear. Gamma-ray background radiation
- **Primordial Fireball** ~380,000 yrs
- Asymmetry between matter and anti-matter: $10^9+1:1$
- $n \rightarrow p + e^- + \bar{\nu}$ half-life ~10.5 mins
- deuterium bottleneck (unstable)
- After 3 mins, photon didn't break deuterium
- $p : n \sim 6 : 1$, $n + \text{deuterium} \rightarrow \text{helium}$
- After 15 mins, **nucleosynthesis** stop
- Only H: He~9:1, little Li, Be



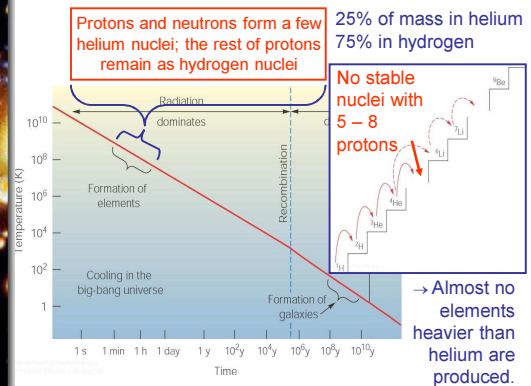
The History of the Universe

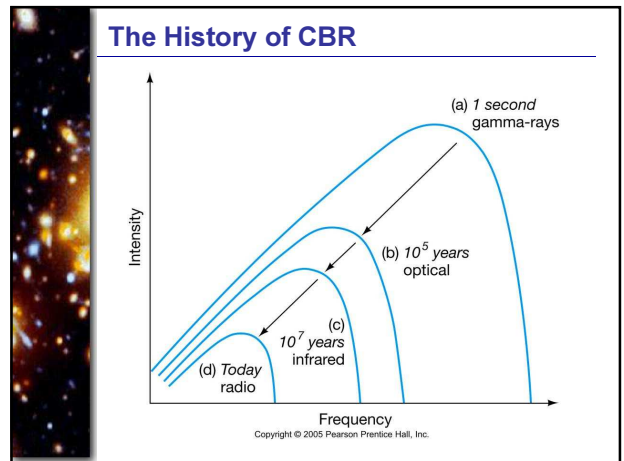
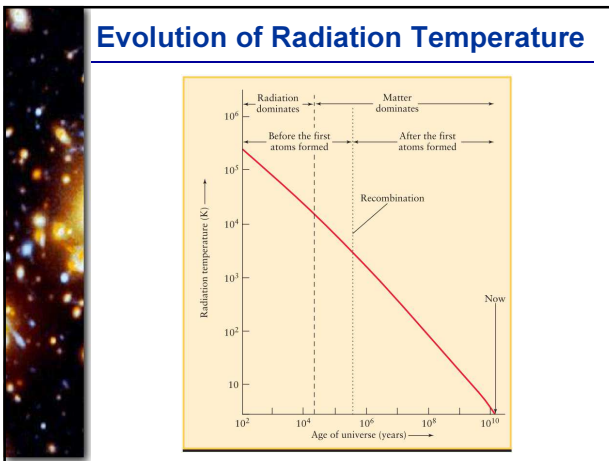
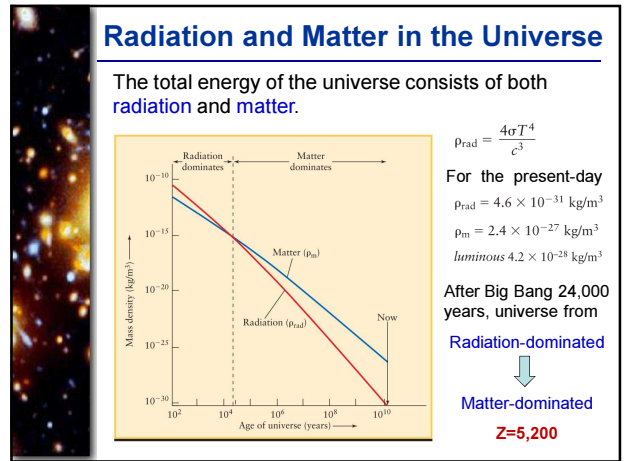
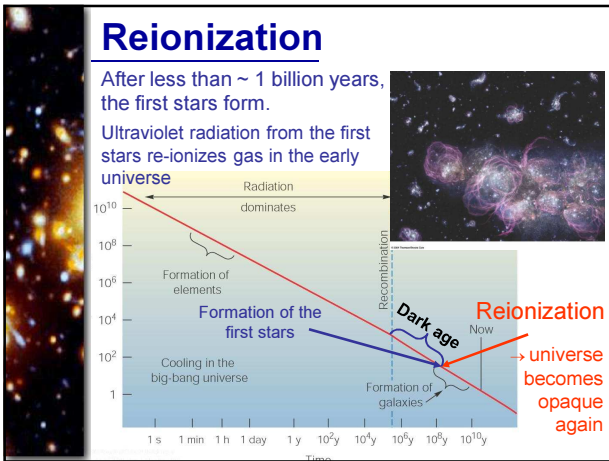
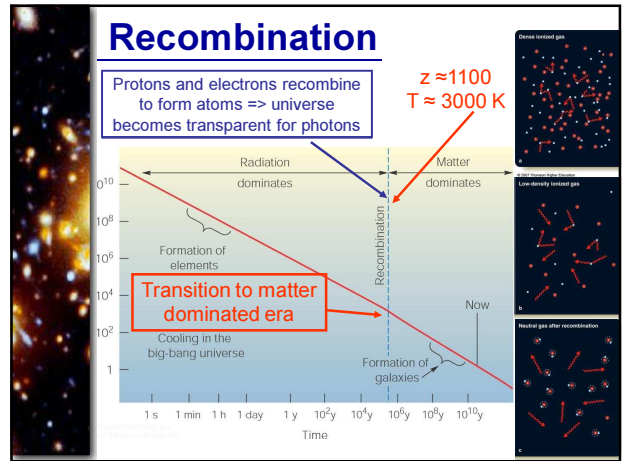
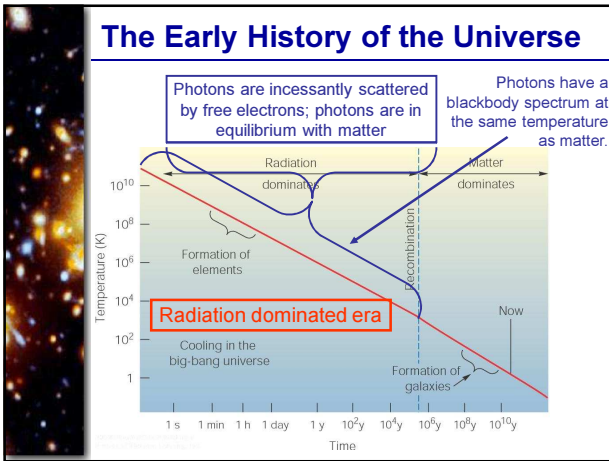


The Early History of the Universe

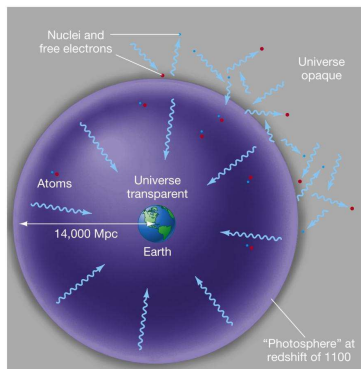


The Early History of the Universe



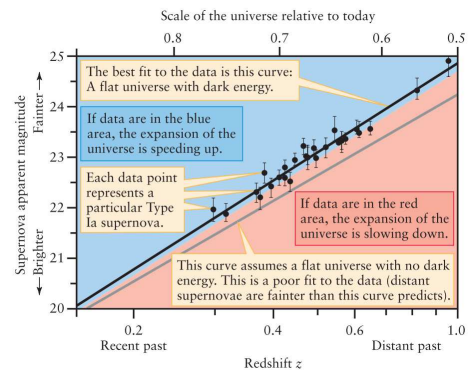


Origin of the CBR: Scattering Surface



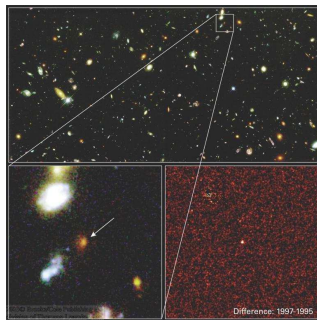
Copyright © 2005 Pearson Prentice Hall, Inc.

The Accelerating Universe



Confirmation of the Acceleration

Observation of the high-red-shift ($z = 1.7$) SN Ia SN1997ff seems to confirm the acceleration of the universe.



The Nobel Prize in Physics 2011

“for the discovery of the accelerating expansion of the Universe through observations of distant supernovae”



Photo: Ariel Zambelich, Copyright © Nobel Media AB
Saul Perlmutter



Photo: Belinda Prattin, Australian National University
Brian P. Schmidt



Photo: Homewood Photography
Adam G. Riess

The Cosmological Constant

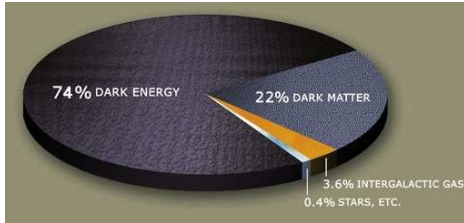
- Cosmic acceleration can be explained with the “Cosmological Constant”, Λ (upper-case lambda)
- Λ is a free parameter in Einstein's fundamental equation of general relativity; previously believed to be 0.
- Energy corresponding to Λ can account for the missing mass/energy ($E = mc^2$) needed to produce a flat space-time.

→ **“Dark Energy”**

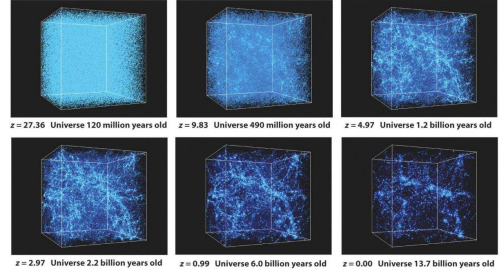
Cosmological Parameters from 2013 Planck results

Age of the universe (Ga)	Hubble's constant ($\text{km}^3/\text{Mpc} \cdot \text{s}$)	Physical baryon density	Physical cold dark matter density
13.819	67.11	0.022068	0.12029
Dark energy density	Density fluctuations at $8h^{-1}\text{Mpc}$	Scalar spectral index	Reionization optical depth
0.6825	0.8344	0.9624	0.0925

Estimated distribution of Matter and Energy in the Universe

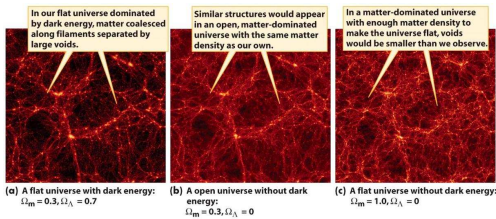


Simulation of the Formation of Large-scale Structures

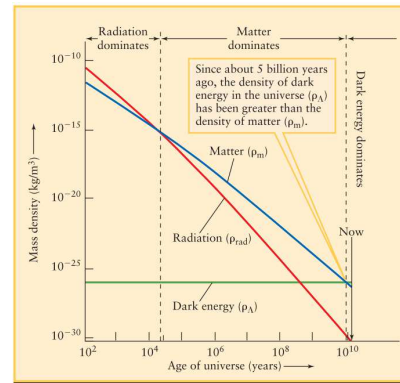


Structures in the Universe

Models based on dark energy and cold dark matter give good agreement with details of the large-scale structure



Evolution of Density, Revisited



Thank you for your attention
Q & A